REPORT DOCUMENTATION PAGE

Form Approved OMB No. 0704-0188

Public reporting burden for this collection of information is estimated to average 1 hour per response, including the time for reviewing instructions, searching existing data sources, gathering and maintaining the data needed, and completing and reviewing the collection of information. Send comments regarding this burden estimate or any other aspect of this collection of information, including suggestions for reducing this burden, to Washington Headquarters Services, Directorate for Information Operations and Reports, 1215 Jefferson Davis Highway, Suite 1204, Arlington, VA 22202-4302, and to the Office of Management and budget, Paperwork Reduction Project (0704-0188), Washington, DC 20503

1. AGENCY USE ONLY (Leave blank)	2. REPORT DATE	3. REPORT TYPE AND DATES O	OVERED
	20 June 1996	Final	
	ixed Defended Ground fect, Non-Instantane		5. FUNDING NUMBERS F04701-93-C-0094
C. Christopher Re	ed		
7. PERFORMING ORGANIZATION The Aerospace Corp. 0. Box 92957, Lo		-2957	8. PERFORMING ORGANIZATION REPORT NUMBER N/A
9. SPONSORING/MONITORING AND SMC/XRES 2420 Vela Way, States Los Angeles AFB,		S)	10. SPONSORING/MONITORING AGENCY REPORT NUMBER N/A
11. SUPPLEMENTARY NOTES N/A			
12a. DISTRIBUTION/AVAILABILIT Distribution Stat Public Release		Approved for	12b. DISTRIBUTION CODE
40 40000400444			

13. ABSTRACT (Maximum 200 words)

These models explore interactions among (a) Weapon systems, (b) Intelligence, Surveillance, and Reconnaissance (ISR) capacity, accuracy, and timeliness, (c) Concepts of Operation, and (d) Scenarios. These interactions allow us to estimate the sensitivity of top-level Measures of Effectiveness (MOEs such as BLUE losses and time taken to achieve BLUE's operational objective) to factors such as

Improved weapons Pk at longer range; Improved ISR/Battle Damage Assessment (BDA) capability; RED ISR/BDA deception tactics; Improved ISR/BDA counter-deception capabilities; Alternative concepts of operation (as defined by parameters such as number of targets attacked per wave, attacker weapon mix, etc.); Changes in scenario parameters (e.g., total numbers of targets and non-targets).

The effects of imperfect, non-instantaneous ISR/BDA on combat attrition are captured by a set of target states which combine BLUE perception, ground truth, and recent target history. Target state populations after the (n+1)st wave are computed from target state populations after the nth wave via functional dependencies involving the attrition, ISR/BDA, OPS concept, and scenario models used. By tracking these target state populations with time, one can unravel the chains of cause-and-effect that lead to the (sometimes counterintuitive) sensitivities of MOEs to the various parameters mentioned earlier.

	els, ISR, BDA, Intel connaissance, Battle		15. NUMBER OF PAGES
	Attacks vs. Ground T		16. PRICE CODE
17. SECURITY CLASSIFICATION OF REPORT Unc 1	18. SECURITY CLASSIFICATION OF THIS PAGE Unclassified	19. SECURITY CLASSIFICATION OF ABSTRACT Unclassified	20. LIMITATION OF ABSTRACT Unlimited

NSN 7540

19960715 136

Standard Form 298 (Rev. 2-89) Prescribed by ANSI Sta. 239-18 298-102

Air Attacks vs. Fixed, Defended Ground Targets:

Imperfect, Non-Instantaneous ISR/BDA Combat Models with

Dr. C. Christopher Reed Modeling & Simulation Department June 20, 1996



Objectives

attempting to take stochastic effects into account. We wanted to learn as much as possible regarding assumptions, ground targets. This allowed us to focus exclusively on the capability of ISR/BDA to distinguish a target from a between combat and ISR/BDA. For this reason a very simple scenario was chosen, i.e., air attacks against fixed outcomes, from this simple model before starting to introduce additional effects. And of course we wanted to tracking. To simplify the problem even further we deliberately used an expected-value approach, rather than The purpose of this exploratory model was to begin getting a better understanding of the interaction non-target or dead target, without having to consider other ISR dimensions such as age of data or target cause-and-effect, target state structure, BLUE perception vs. ground truth, and their impacts on combat understand the extent to which the insights gained from this model can be extrapolated to more complex

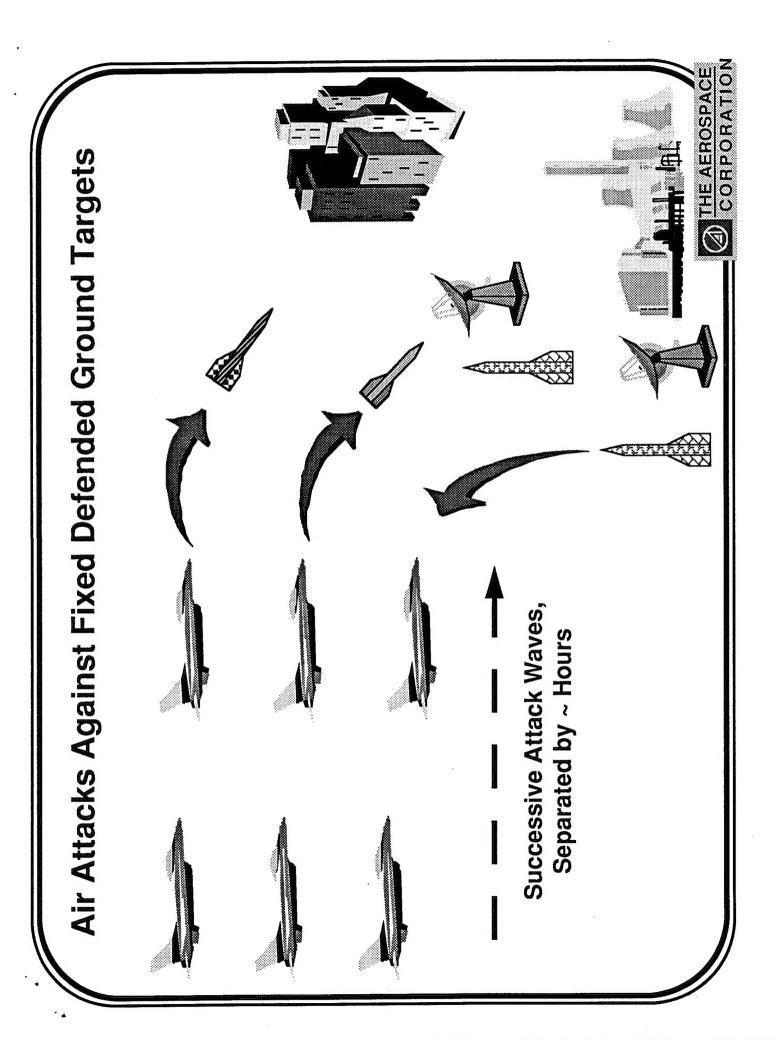
Objectives

- Exploratory Modeling to begin getting insight into impact of ISR on combat outcomes; Heavy parametric flavor; Walk before run:
- Fixed Ground Targets -> No age of data, No tracking
- Focus on impacts of False Positives, False Negatives
- No stochastic effects. Use probabilities only to compute expected values
- are not captured? What kinds of subtleties arise in even simple models? Which conclusions make sense? Which don't? What important effects
- Identify/Understand chains of cause and effect that link inputs and assumptions to outputs
- What kind of target state structure is needed to capture the impact of ISR on combat?
- In what ways do discrepancies between BLUE's perceptions and the ground truth impact combat outcomes?



Air Attacks Against fixed Defended Ground Targets

The scenario analyzed involves successive waves of attackers striking fixed ground targets that are defended. The defenders might be SAM sites, or AA batteries, for example. BLUE's objective is to kill some fraction, say 50%, of all the RED targets.

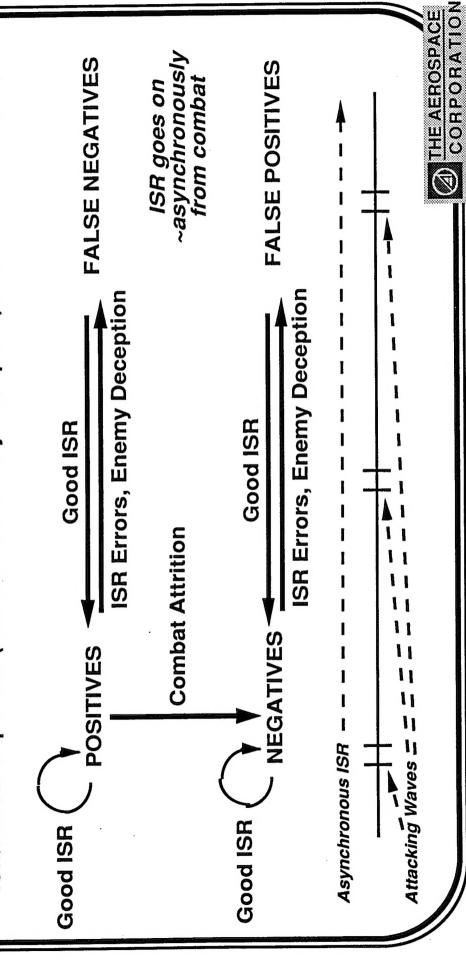


Essential Features Modeled

kill, and Negatives are things he's not interested in. False Positives and False Negatives arise when BLUE mistakes a Positive for a Negative, or vice-versa. ISR capability in this model is defined by how well BLUE can distinguish Positives from Negatives, and how quickly it can do this. ISR/BDA will degrade due to deception by more or less continuously and asynchronously from the combat activities. Positives are things BLUE wants to At the same time that BLUE is sending out successive waves to attack RED, there is ISR/BDA going on the enemy, or due to the extent to which Positives are mistaken for Negatives (or vice-versa).

Essential Features Modeled

- BLUE Attacks RED in waves, usually separated by hours Each BLUE wave attacks only a subset of RED (i.e., M targets)
 - RED DEFENDERS shoot at BLUE and vice-versa
- Attacking BLUE Aircraft have Resource Constraints
- ISR/BDA is Imperfect (ISR Errors + Enemy Deception) and Non-Instantaneous



Air-To-Ground Combat Model • Additional Features

more targets to his attack list so as to end up attacking the desired number of Positives. At present this estimate is estimate of the extent to which the targets he attacks on any given wave will include False Positives, and to add some constant percent, but it could be made to vary from wave to wave depending on some criteria (e.g., how fixed number of "targets", some of which may in fact be False Positives. The model allows BLUE to make an The way the model is set up, there are a fixed number of attacking aircraft per wave, and they attack a many of the "targets" attacked had defenders that shot back).

In the interest of simplicity, the attrition model is the Lanchester model for directed fire, with appropriate Pk's and firing rates. If BLUE runs out of ammunition he turns around and leaves, and attrition is stopped

AIR-TO-GROUND COMBAT MODEL

Additional Features

- Fixed numbers of aircraft per attacking wave
- Each wave attacks some number (i.e., subset) of RED Targets
- Planning/Resource Allocation for each wave based on ISR/BDA following attack by previous wave
- N Defenders per target. Only defenders whose targets are being shot at will shoot back.
- Eventually, more sophisticated probabilistic attrition models will be used At present, Lanchester attrition model for directed fire is used.
- Combat Model uses Pk's and Firing Rates for

BLUE vs. Fixed RED Targets

BLUE vs. RED Defenders (different weapons than vs. RED Targets)

RED Defenders vs. BLUE

Engagement times may be constrained by weapon-carrying capacity of attacking aircraft



Examples of Types of Input Parameters

As this chart indicates, this model is really four models in one -- Weapons System, OPS Concept, ISR/BDA, and Scenario. The parameters listed are not all of the parameters, but are the ones that are of most interest.

Examples of Types of Input Parameters

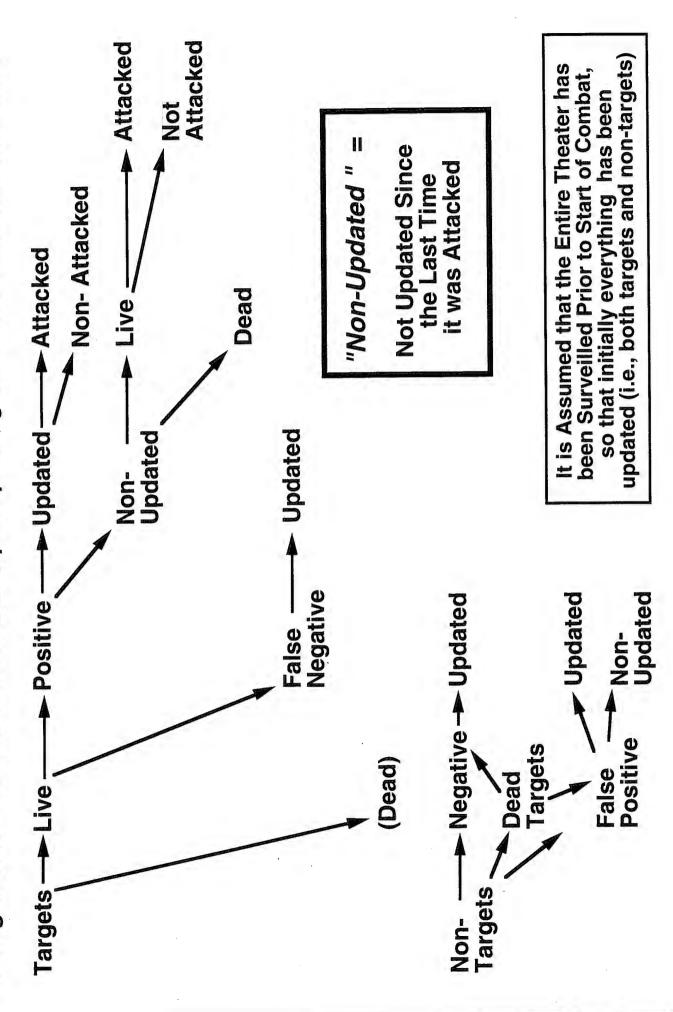
Weapon System	OPS Concept	ISR/BDA	Scenario
• RED & BLUE PKs	• # A/C per Wave	Probabilities thatPOS mistaken for NEG	• # Targets
• RED & BLUE Firing Rates	• # Targets attacked per wave	- NEG mistaken for POS	• # Non- Targets
• # Weapons per A/C	• Time between successive waves	• ISR Update Rates	• # Defenders per target
Run Control	Stop if % RED su Stop if BLUE kill	 Stop if % RED surviving drops below threshhold Stop if BLUE killed exceeds threshhold 	w threshhold nold

Decomposition of ISR Target States

targets it is not necessary to distinguish between Attacked and Non-Attacked, since attacking a non-target will not distinguish between targets that get attacked during a given wave, and those that don't get attacked. Similarly, the non-targets can be either Negatives or False Positives, either of which may be updated or non-updated. For non-(which become non-targets); live targets may be Positives or False Negatives, which in turn may be updated or One of the key parts of this analysis involves setting up a suitable set of ISR/BDA target states. The need non-updated; Non-updated Positives may in fact be either live or dead; and for the Positives one has to further processes. Thus it is necessary to distinguish first between targets and non-targets; targets may be live or dead for these states is driven by the need to keep track of what happens during both the attrition and ISR/BDA

Decomposition of ISR Target States

Target States are functions of BLUE perception, ground truth, and recent history



Evolution of ISR Target States • Example: Updated Positives

Attacked and Non-Attacked) will get updated by ISR/BDA, some won't, and of those that get updated, some will Positives. These are Positives that have been attacked, have survived the attack, and have been updated correctly some will be live and some dead after the attack. Prior to the start of the next wave some of these targets (both To illustrate how this target state decomposition works in practice, consider the example of the Updated by ISR/BDA as Positives. During the next attack some of there get attacked, and some don't, and as a result, get updated correctly and some won't.

populations prior to the (n+1)st wave -- i.e., add up all of the Updated Positives, all of the Updated Negatives, and The result of all of this is that the Updated Positives will split into a variety of different states -- Updated Negative, Updated False Positive, Dead non-Updated Positive, etc. One needs to go through and do this same kind of analysis for each of the different target state populations, and then re-combine each of the state so on, in order to come up with the target state populations prior to the start of the next wave.

Evolution of ISR Target States • Example: Updated Positives

Dead Non-Updated Target State False Negative Updated False Positive Non-Updated Resulting Negative Updated Positive Updated Positive Updated Updated Positive Updated Positive Positive No Change Incorrectly Incorrectly Updated Correctly **Uncertain Uncertain** Result of BDA Correctly Updated -Updated Updated Updated Not ____ Updated Updated During BDA Updated -Not ____Updated Updated Updated Not of Attack Attacked Result Attacked During Attacked Attack nth Attack Updated Before Positive

Updated False Negative

Incorrectly

Updated

Correctly

List of ISR Target States

Attacked and Non-Attacked. Non-Updated targets, on the other hand, are targets that have been attacked but not combination of ground truth, BLUE perception, and recent history. Targets split into True Positives and False Negatives; the True Positives split further into Updated and Non-Updated. The Updated ones split further into So the final list of ISR Target states that one ends up with is shown here. As indicated, these states are a updated by ISR/BDA. Thus they may be either live or dead, and this poses a problem for BLUE, because he doesn't know how may are live, and how many are dead. He may have to waste resource re-attacking dead

impossible to attack a Negative. Should BLUE decide to attack a Negative, he would immediately, by his decision Updated" applies only to something that has been attacked but not updated since the attack. But by definition it's to attack it, turn it into a False Positive. Similarly, it is impossible to attack a False Negative. To do so would Observe that there are no Non-Updated Negatives or False Negatives. This happens because "Nonautomatically turn it into a Positive.

List of ISR Target States

- TARGETS
- True Positive
 Updated True Positive

Updated True Positive Attacked Updated True Positive Not Attacked

Non-Updated True Positive

Non-Updated True Positive Live Non-Updated True Positive Live

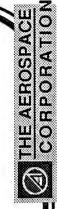
Not Attacked Attacked Non-Updated True Positive

Non-Updated Positive Dead

False Negative
 Updated False Negative

- NON-TARGETS
- True Negative
 Updated True Negative
- ନିಷାର**୍ଚ Positive** Updated ନି**ಷା**ଛ୍ଡ *Positive* Non-Updated ନିଛାର୍ଚ୍ଚ *Positive*

Ground Truth = Outline
BLUE Perception = Italics
Recent History = Bold



How Model Is Put Together -- Key Ideas

To illustrate how the target state populations are computed, consider the set of Updated True Positives.

fraction of these attacked "targets" that had been updated prior to the attack. Then the number of these that are BLUE attacks some number m0 of "targets" (real targets plus non-targets) per wave. Let p1 be the Updated True Positives is given by (2) -- it's some fraction of m0 p1.

To compute how many of these survive the attack, one needs to subtract off the attrition suffered during the attack. Of these that survive, some fraction will get updated by BDA prior to the next attack, and of these, some fraction will get updated correctly, becoming part of the population of True Positives prior to the next attack.

How Model is Put Together -- Key Ideas

Example: Start with Updated (True) Positives

Blue Perceptions are in Italics

- Let p₁ = Fraction of Attacked Positives That Had Been Updated Prior to the (1) Assume mo Positives (Both Updated and Non-Updated) Get Attacked per Wave Attack (an OPS Concept Variable)
- (2) Then # Updated (True) Positives That Get Attacked

(# Updated Positives)

 $m_0 p_1$

(# Updated Positives + # Updated False Positives)

- (3) # Of These That Survive Attack = (2) Attrition of Updated Positives During Attack
- (4) Fraction of (3) That Get Updated by BDA Subsequent to Attack =
- (3) X Probability of Getting Updated (This Is a Function of BDA Update Rate and Time Between Waves)
- (5) Fraction of (4) That Get Updated Correctly =
- (4) X Probability of Getting Updated Correctly (an ISR Performance
- ⇒ These Become Updated (True) Positives

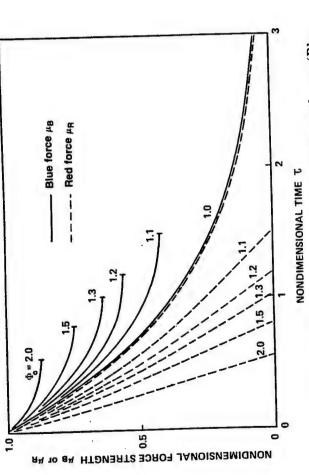


BLUE Superiority Parameter

Before discussing some of the results that come out of this model, it is helpful to understand the role of the RED force strengths vs. non-dimensional time for different values of the superiority parameter. The greater the fewer the BLUE losses per RED killed. What this means in practice is that an attacker would always try to have BLUE superiority parameter, the shorter the engagement (i.e., the time needed to kill all of the RED), and the superiority parameter in the Lanchester model. The superiority parameter involves the ratio of the force sizes, and the square root of the ratio of the Pk's times the firing rates. The plot shows non-dimensional BLUE and enough in the way of force size and firepower so as to ensure an adequate superiority parameter during an engagement. Observe also that the superiority parameter is linear in brute force (i.e., force size), but goes as the square root of technology (Pk's and firing rates).

BLUE Superiority Parameter

$$\Phi_0 = \frac{\# BLUE}{\# RED} X_{\sqrt{}} \frac{BLUE}{RED} \frac{P_k}{P_k} \frac{x}{x} \frac{BLUE}{RED} \frac{FIRING}{FIRING} \frac{RATE}{RATE}$$



Lanchester Model for Directed Fire

Variation of the nondimensional force strength μ_B (Blue forces) or μ_R (Red forces) with the nondimensional time τ for $\Phi_0 \ge 1$ (directed fire combat).



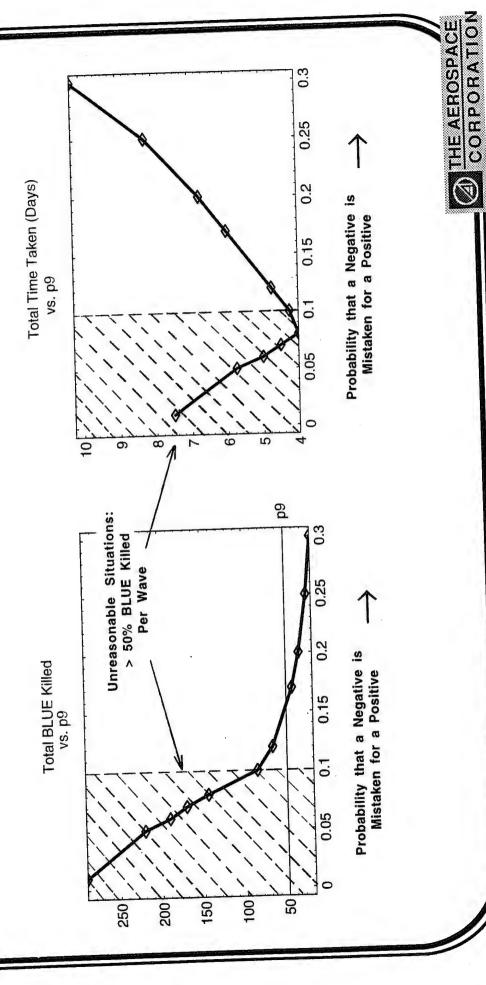
Total BLUE Killed and Total Time Taken vs. Probability that a Negative is Mistaken for a Positive

this is a parametric model, it is possible to vary each parameter independently, sometimes in ways that would be completely unreasonable The next three charts show some of the results that illustrate some of the main impacts of ISR/BDA on combat (within the context attacking aircraft per wave. These types of operational constraints have, for the most part, been deliberately left out of the model in order of the present model!). In viewing these charts, it is very important to understand what was varied and what was held constant. Because to better probe the cause-and effect relationships between the various parameters and outputs. Although this approach does require some from an operational point of view. Even though some of the situations one encounters when doing this are operationally unreasonable, nevertheless they are valuable from the point of view of analysis because of the insights they yield. In practice when one parameter is varied, other parameters would be varied together with it; for example, if more targets are attacked per wave, one would also use more mental adjustment on the part of the reader or analyst, it yields insights that might otherwise be missed if other constraints and assumptions were implicitly built into the model.

Recall that the way the model is set up, a fixed number of aircraft attack a fixed number of "targets". What is not fixed, however, is the ratio of real targets to false targets (or non-targets) within this fixed number attacked. The firing rates, Pk's, and force sizes were deliberately set so that if all of the attacked "targets" were in fact real targets, then all of the BLUE attackers would get killed and RED losses would be minimal. This was done intentionally in order to better see the effect of diluting the set of attacked RED targets with False Positives, which would have the effect of shifting the superiority parameter in BLUE's favor. More specifically, let p9 be the probability that a non-target is mistaken for a real target. Here we had 500 targets and 5000 non-targets, so p9 = 0.1 meant that there were $0.1 \times 5000 = 500$ false positives, in addition to the 500 real targets. As p9 increases, the ratio of real targets to false positives decreases, so in any attack against a fixed number of "targets" there will be progressively fewer real targets attacked. Thus the BLUE/RED force ratio will be greater, and there will be fewer BLUE losses per RED killed, hence the total BLUE killed will decrease as p9 increases.

as follows: For small values of p9 BLUE is out gunned and all BLUE are killed on every wave. As p9 initial increases BLUE is still out On the other hand, the total time taken for BLUE to accomplish its objective has a minimum near p = 0.1. The reason for this is gunned, but not quite as badly, and is able to kill more of RED on each wave, before getting wiped out by RED. As p9 is increased yet further, the percentage of real targets attacked in each wave gets diluted further, until eventually BLUE is no longer out gunned. At this point BLUE is able to start killing all of the RED targets it attacks in each wave. But as the percentage of RED targets attacked in each wave decreases (due to increasing p9), it takes more waves in order for BLUE to accomplish its objective.

Total BLUE Killed and Total Time Taken vs. Probability that a Negative is Mistaken for a Positive



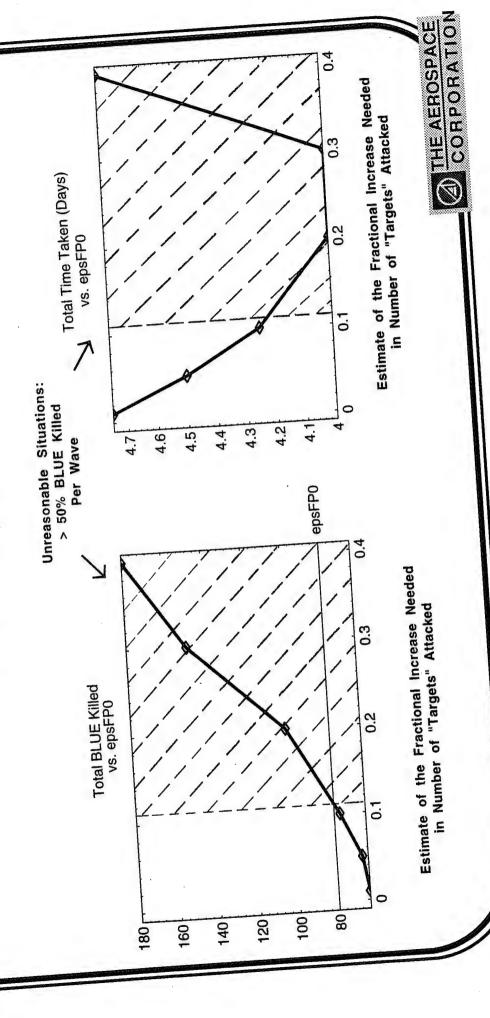
Total Blue Killed and Total Time Taken vs. BLUE's Estimate of the Fractional Increase Needed in Number of "Targets" Attacked to Ensure that the Desired Number of Real Targets get Attacked

epsFP0 is BLUE's estimate of the fractional increase needed in the number of "targets" attacked to ensure that out of the total number of "targets" attacked, the desired number of them will be real targets. For a fixed ratio of real targets to False Positives, as epsFP0 is increased, more and more real targets will be attacked per wave, hence BLUE losses will increase with epsFP0.

On the other hand, when epsFP0 is small, a relatively small number of real targets will be attacked per wave, and more waves will be required for BLUE to achieve its objective.

with the result that BLUE losses per wave become very high, while RED losses per wave decrease. When this decreases. Eventually, however, BLUE gets to the point of having to take on too many real targets per wave, As epsFP0 is increased, BLUE encounters more real targets per wave, and so the total time required starts to happen, the total time taken becomes an increasing function of epsFP0.

"Targets" Attacked to Ensure that the Desired Number of Estimate of the Fractional Increase Needed in Number of Total BLUE Killed and Total Time Taken vs. BLUE's Real Targets get Attacked



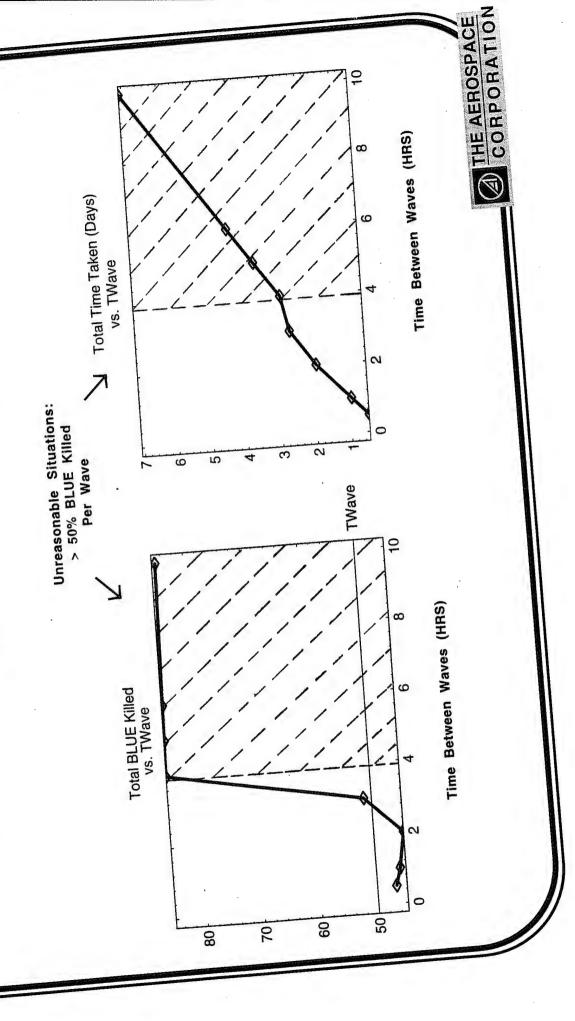
Total Blue Killed and Total Time Taken vs. Time Between Waves

between waves, resulting in a more dilute "target" set, and fewer BLUE losses. For the parameters used here, the When the target attack rate (i.e., number of targets attacked per wave divided by the time between waves) eventually BLUE will run out of updated targets to attack (recall that initially everything has been updated), and will have to attack mostly non-updated (hence possibly dead) targets, plus the few positives that get updated target attack rate exceeds the target update rate once the time between waves drops below about four hours. is greater than the ISR/BDA target update rate, in other words, when the time between waves is very short

avoid attacking too many non-updated targets. But since the number of attacking aircraft is being held fixed, this rate, then we get a "richer" target set because enough targets are getting updated between waves for BLUE to Once the target attack rate slows down to the point where it's less than or equal to the ISR/BDA update has the effect of decreasing BLUE's superiority parameter, thus increasing BLUE losses per target attacked, which leads to more total BLUE losses. On the other hand, the total time taken is a more or less linear function of the time between waves because it equals the number of waves times the time between waves. When the time between waves is very short, BLUE or live) between waves, which means that more dead targets are getting confirmed as dead, which in turn means waves. This happens because more and more of the attacked targets are getting updated (and confirmed as killed ends up attacking a more dilute "target" set, as discussed above, which means that it takes relatively more waves for BLUE to accomplish its goal. Once the time between waves is long enough so that the target attack rate no longer exceeds the ISR BDA target update rate, then total BLUE killed drops slightly with the time between that the pool of False Negatives increases more slowly.

losses and less time taken, even though each attack is less efficient. As mentioned above, the time between waves between waves drops below two hours is an artifact of the model: the model only checks total RED killed at the Observe also that a fast OPS Tempo (for example, one to two hours between waves) leads to less BLUE end of each wave, and thus it is possible for it to "overshoot" its goal slightly if it was a fraction of a percent has a potent multiplicative effect on the total time taken. The slight increase in total BLUE killed as the time short of 50% RED killed on the previous wave. But more RED killed also means more BLUE killed.

Total BLUE Killed and Total Time Taken vs. Time Between Waves

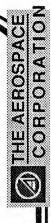


Impact of ISR/BDA on Distribution of Target States

As indicated on the chart, there are various ways in which imperfect ISR/BDA can increase the number of False Positives. It can also make it harder to find the True Positives, and it can cause dead targets to get attacked probability of updating a dead target to a positive, but the better the ISR/BDA capability, the slower this ratio again. The ratio of Positives to False Positives will always decrease with time due to RED attrition plus the will decrease.

Impacts of ISR/BDA on Distribution of Target States

- BLUE's list of Positives may include an increasing number of False Positives due to
- Increased Probability of mistaking a Negative for a Positive (especially if many Negatives are present)
- Increased Probability of mistaking a dead target for a live one
- High ISR/BDA update rate (more dead targets updated per unit time some will be updated to Positives)
- Positives can be harder to find due to increased probability of mistaking a Positive for a Negative
- Dead Targets (that have been previously attacked) get attacked again if
- Time between waves is too short
- Update rate is too slow
- Ratio of Positives to False Positives decreases with time due to RED attrition plus probability of dead targets being updated to Positives



Operational Impacts of Imperfect ISR/BDA

his superiority parameter in either of two ways: (a) attack fewer targets per wave, which is equivalent to trading In order to cope with the uncertainties produced by the presence of False Positives, BLUE needs to "pad" losses vs. total time, or (b) add more resources to each wave.

Increasing the OPS Tempo has a generally positive effect, as noted.

technology, technology may be less expensive, especially when one considers the potential "costs" of casualties, And even though the superiority parameter is linear in brute force, while it goes as the square root of POWs, and hostage situations.

Operational Impacts of Imperfect ISR/BDA

- In planning an attack, BLUE wants a reasonable superiority parameter
- If BLUE underestimates RED False Positives (including dead targets) he will use more resources than necessary
- If BLUE overestimates RED False Positives, he will be outgunned
- BLUE can achieve a reasonable superiority parameter in two ways:
- By attacking fewer targets per wave (with same number of attackers) => fewer losses but more total time required (trade losses vs. time)
- To be on the safe side BLUE can "pad" superiority parameter by adding more resources to each wave -- wasteful but safer
- Positives attacked) because both casualties and total time taken are less update rate may still pay off (despite inefficient operation -- more False Increased OPS tempo (time between waves) without increased BDA
- Brute force (more A/C, faster OPS tempo, fewer targets attacked per wave) has more impact on "padding" the superiority parameter than technology (Pk's, firing rates). Superiority parameter is linear in brute force, but goes as square root of technology. But technology may be less expensive.



Utility of Improved ISR/BDA

the time and associated cost of accomplishing a mission, (c) reduce the technology requirements (associated with As noted, improved ISR/BDA can (a) reduce the resources required to accomplish a mission, (b) reduce a technology solution to increasing the superiority parameter) to the point where the technology solution becomes feasible.

Utility of Improved ISR/BDA

- More efficient use of BLUE resources. Less "pad" needed per wave to ensure adequate BLUE superiority parameter.
 - => Do same job with fewer resources
- Gives BLUE more flexibility to trade brute force for technology => Technology solution may be cheaper
- Reduces total time taken to accomplish BLUE objective => Less total expense
- Improves efficiency of fast OPS Tempo, and permits yet faster OPS
 - => Less total time taken => Less total expense
- limit the extent to which BLUE can take advantage of improved ISR/BDA In actual practice there may be a variety of operational constraints that



Lessons Learned

coupled with the nonlinearities produced by the inclusion of both BLUE perceptions together with Ground Truth of the challenges that can be expected with more complex models. And it is clear that the target state structure is into the underlying cause-and-effect mechanisms, with some surprising conclusions (which, of course, should be interpreted in the light of the simple assumptions used). As an exploratory model, it provides a good indication in estimating expected values. Despite these difficulties, it was possible to get a considerable amount of insight position, target velocity, position and velocity uncertainties, age of data, target tracking, IFF, assessing target This turned out to be a very complex problem, mainly because of the non-trivial target state structure, something that needs to be analyzed very carefully when other aspects of ISR performance (such as target intent, and so on) are taken into account.

role in a probabilistic analysis of the problem, since in the latter case one is attempting to compute distributions On the other hand, it's not clear that the above-mentioned nonlinearities would necessarily play the same of outcomes, rather than expected values. This is something that requires further research and analysis.

Lessons Learned

- Seemingly simple problem turned out to be very complex, with many subtleties
- BLUE perception vs. Ground Truth in computing Expected Values is source of considerable non-linearity
- Target states need to include Blue Perception, Ground Truth, plus some recent history
- Complexity of target state structure drives complexity of analysis
- Expressions for target state populations are algebraically complex, nonlinear, and opaque
- Nevertheless, chains of cause-and-effect can be inferred, leading to some unexpected conclusions
- Fire Lanchester Model, Fixed Targets, and True/False Positive/Negative Conclusions driven largely by simple assumptions used, i.e., Directed Target States.
- Some conclusions may extrapolate to more complex situations, others probably won't.

